

# Vidyasagar University

## Curriculum for B.Sc. Honours in Mathematics [Choice Based Credit System]

### Semester-I

| Sl.No.                    | Name of the Subject                             | Nature        | Code | Teaching Scheme<br>in hour per week |   |   | Credit | Marks |
|---------------------------|---|---------------|------|-------------------------------------|---|---|--------|-------|
|                           |   |               |      | L                                   | T | P |        |       |
| C1                        | C1T:Calculus,Geometry&<br>Differential Equation | Core Course-1 |      | 5                                   | 1 | 0 | 6      | 75    |
| C2                        | C2T: Algebra                                    | Core Course-2 |      | 5                                   | 1 | 0 | 6      | 75    |
| GE-1                      | GE-1  | GE            |      |                                     |   |   | 4/5    | 75    |
|                           | GE-1  | GE            |      |                                     |   |   | 2/1    |       |
| AECC                      | English   | AECC          |      |                                     |   |   | 2      | 50    |
| <b>Total Credits = 20</b> |   |               |      |                                     |   |   |        |       |

**AECC- Ability Enhancement Compulsory Course:** English /Modern Indian

Language **Interdisciplinary/Generic Elective (GE) from other Department**

**[Four papers are to be taken and each paper will be of 6 credits]:** Papers are to be taken from any of the following discipline: **Physics/Chemistry/Computer Sc/Statistics /Geology/Electronics/Economics /Physiology /Bio-technology**

# Semester-1

## Core Course

### Core -1

**CC-1: Calculus, Geometry & Differential Equation**

**Credits 06**

### Core T1 – Calculus, Geometry & Differential Equation

| Calculus, Geometry & Differential Equation   |           |
|--|-----------|
|  | 6 Credits |
| Unit 1   |           |
| Hyperbolic functions, higher order derivatives, Leibnitz rule and its applications to problems of type $e^{ax+b}\sin x$ , $e^{ax+b}\cos x$ , $(ax+b)^n\sin x$ , $(ax+b)^n\cos x$ , concavity and inflection points, envelopes, asymptotes, curve tracing in cartesian coordinates, tracing in polar coordinates of standard curves, L'Hospital's rule, applications in business, economics and life sciences.                                  |           |
| Unit 2   |           |
| Reduction formulae, derivations and illustrations of reduction formulae of the type $\int \sin nx \, dx$ , $\int \cos nx \, dx$ , $\int \tan nx \, dx$ , $\int \sec nx \, dx$ , $\int (\log x)^n \, dx$ , $\int \sin^n x \cos^m x \, dx$ , parametric equations, parameterizing a curve, arc length of a curve, arc length of parametric curves, area under a curve, area and volume of surface of revolution, techniques of sketching conics. |           |
| Unit 3   |           |
| Reflection properties of conics, rotation of axes and second degree equations, classification of conics using the discriminant, polar equations of conics.<br><br>Spheres. Cylindrical surfaces. Central conicoids, paraboloids, plane sections of conicoids, generating lines, classification of quadrics, illustrations of graphing standard quadric surfaces like cone, ellipsoid.  |           |
| Unit 4   |           |

Differential equations and mathematical models. General, particular, explicit, implicit and singular solutions of a differential equation. Exact differential equations and integrating factors, separable equations and equations reducible to this form, linear equation and Bernoulli equations, special integrating factors and transformations.

#### Graphical Demonstration (Teaching Aid)

1. Plotting of graphs of functions  $e^{ax+b}$ ,  $\log(ax + b)$ ,  $1/(ax + b)$ ,  $\sin(ax + b)$ ,  $\cos(ax + b)$ ,  $|ax + b|$  and to illustrate the effect of a and b on the graph.
2. Plotting the graphs of polynomial of degree 4 and 5, the derivative graph, the second derivative graph and comparing them.
3. Sketching parametric curves (Eg. trochoid, cycloid, epicycloids, hypocycloid).
4. Obtaining surface of revolution of curves.
5. Tracing of conics in cartesian coordinates/ polar coordinates.
6. Sketching ellipsoid, hyperboloid of one and two sheets, elliptic cone, elliptic, paraboloid, and hyperbolic paraboloid using cartesian coordinates.

#### [ Reference Books]

- ▶ G.B. Thomas and R.L. Finney, Calculus, 9th Ed., Pearson Education, Delhi, 2005.
- ▶ M.J. Strauss, G.L. Bradley and K. J. Smith, Calculus, 3rd Ed., Dorling Kindersley (India) P. Ltd. (Pearson Education), Delhi, 2007.
- ▶ H. Anton, I. Bivens and S. Davis, Calculus, 7th Ed., John Wiley and Sons (Asia) P. Ltd., Singapore, 2002.
- ▶ R. Courant and F. John, Introduction to Calculus and Analysis (Volumes I & II), Springer- Verlag, New York, Inc., 1989.
- ▶ S.L. Ross, Differential Equations, 3rd Ed., John Wiley and Sons, India, 2004.
- ▶ Murray, D., Introductory Course in Differential Equations, Longmans Green and Co.
- ▶ G.F. Simmons, Differential Equations, Tata Mcgraw Hill.
- ▶ T. Apostol, Calculus, Volumes I and II.
- ▶ S. Goldberg, Calculus and mathematical analysis.
- ▶

## Core -2

### CC-2: Algebra

Credits 06

#### Core T2- Algebra

| Algebra  |           |
|--|-----------|
|  | 6 Credits |
| Unit 1   |           |
| <p>Polar representation of complex numbers, nth roots of unity, De Moivre's theorem for rational indices and its applications.</p> <p>Theory of equations: Relation between roots and coefficients, transformation of equation, Descartes rule of signs, cubic and biquadratic equation.</p> <p>Inequality: The inequality involving <math>AM \geq GM \geq HM</math>, Cauchy-Schwartz inequality.</p>        |           |
| Unit 2   |           |
| <p>Equivalence relations. Functions, composition of functions, Invertible functions, one to one correspondence and cardinality of a set. Well-ordering property of positive integers, division algorithm, divisibility and Euclidean algorithm. Congruence relation between integers. Principles of Mathematical induction, statement of Fundamental Theorem of Arithmetic.</p>                              |           |
| Unit 3   |           |
| <p>Systems of linear equations, row reduction and echelon forms, vector equations, the matrix equation <math>Ax=b</math>, solution sets of linear systems, applications of linear systems, linear independence.</p>  |           |
| Unit 4   |           |
| <p>Introduction to linear transformations, matrix of a linear transformation, inverse of a matrix, characterizations of invertible matrices. Subspaces of <math>\mathbb{R}^n</math>, dimension of subspaces of <math>\mathbb{R}^n</math>, rank of a matrix, Eigen values, eigen vectors and characteristic equation of a matrix. Cayley-Hamilton theorem and its use in finding the inverse of a matrix.</p> |           |
| Reference Books  |           |
| <ul style="list-style-type: none"><li>▶ Titu Andreescu and Dorin Andrica, Complex Numbers from A to Z, Birkhauser, 2006.</li><li>▶ Edgar G. Goodaire and Michael M. Parmenter, Discrete Mathematics with Graph Theory, 3rd Ed.,</li></ul>  |           |

Pearson Education (Singapore) P. Ltd., Indian Reprint, 2005.

- ▶ David C. Lay, Linear Algebra and its Applications, 3rd Ed., Pearson Education Asia, Indian Reprint, 2007.
- ▶ K.B. Dutta, Matrix and linear algebra.
- ▶ K. Hoffman, R. Kunze, Linear algebra.
- ▶ W.S. Burnstine and A.W. Panton, Theory of equations.

## Generic Elective Syllabus

### GE-1 [Interdisciplinary for other department]

**GE-1: Calculus, Geometry & Differential Equation**

**Credits 06**

#### **GE-1T – Calculus, Geometry & Differential Equation**

| Calculus   |           |
|--|-----------|
|  | 6 Credits |
| Unit 1   |           |
| Hyperbolic functions, higher order derivatives, Leibnitz rule and its applications to problems of type $e^{ax+b}\sin x$ , $e^{ax+b}\cos x$ , $(ax+b)^n\sin x$ , $(ax+b)^n\cos x$ , concavity and inflection points, envelopes, asymptotes, curve tracing in cartesian coordinates, tracing in polar coordinates of standard curves, L'Hospital's rule, applications in business, economics and life sciences.                                  |           |
| Unit 2   |           |
| Reduction formulae, derivations and illustrations of reduction formulae of the type $\int \sin nx \, dx$ , $\int \cos nx \, dx$ , $\int \tan nx \, dx$ , $\int \sec nx \, dx$ , $\int (\log x)^n \, dx$ , $\int \sin^n x \cos^m x \, dx$ , parametric equations, parameterizing a curve, arc length of a curve, arc length of parametric curves, area under a curve, area and volume of surface of revolution, techniques of sketching conics. |           |
| Unit 3   |           |
| Reflection properties of conics, rotation of axes and second degree equations, classification of conics using the discriminant, polar equations of conics.   |           |
| Spheres. Cylindrical surfaces. Central conicoids, paraboloids, plane sections of conicoids, generating lines,  |           |

classification of quadrics, illustrations of graphing standard quadric surfaces like cone, ellipsoid.

#### Unit 4

Differential equations and mathematical models. General, particular, explicit, implicit and singular solutions of a differential equation. Exact differential equations and integrating factors, separable equations and equations reducible to this form, linear equation and Bernoulli equations, special integrating factors and transformations.

#### Graphical Demonstration (Teaching Aid)

1. Plotting of graphs of function  $e^{ax+b}$ ,  $\log(ax + b)$ ,  $1/(ax + b)$ ,  $\sin(ax + b)$ ,  $\cos(ax + b)$ ,  $|ax + b|$  and to illustrate the effect of a and b on the graph.
2. Plotting the graphs of polynomial of degree 4 and 5, the derivative graph, the second derivative graph and comparing them.
3. Sketching parametric curves (Eg. trochoid, cycloid, epicycloids, hypocycloid).
4. Obtaining surface of revolution of curves.
5. Tracing of conics in cartesian coordinates/ polar coordinates.
6. Sketching ellipsoid, hyperboloid of one and two sheets, elliptic cone, elliptic, paraboloid, and hyperbolic paraboloid using cartesian coordinates.

#### [Reference Books]

- ▶ G.B. Thomas and R.L. Finney, Calculus, 9th Ed., Pearson Education, Delhi, 2005.
- ▶ M.J. Strauss, G.L. Bradley and K. J. Smith, Calculus, 3rd Ed., Dorling Kindersley (India) P. Ltd. (Pearson Education), Delhi, 2007.
- ▶ H. Anton, I. Bivens and S. Davis, Calculus, 7th Ed., John Wiley and Sons (Asia) P. Ltd., Singapore, 2002.
- ▶ R. Courant and F. John, Introduction to Calculus and Analysis (Volumes I & II), Springer- Verlag, New York, Inc., 1989.
- ▶ S.L. Ross, Differential Equations, 3rd Ed., John Wiley and Sons, India, 2004.
- ▶ Murray, D., Introductory Course in Differential Equations, Longmans Green and Co.

- ▶ G.F.Simmons, Differential Equations, Tata Mcgraw Hill.
- ▶ T. Apostol, Calculus, Volumes I and II.
- ▶ S. Goldberg, Calculus and mathematical analysis.
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# Vidyasagar University

## Curriculum for B.Sc. Honours in Mathematics [Choice Based Credit System]

### Semester-II

| Sl.No.        | Name of the Subject                                       | Nature        | Code | Teaching Scheme in hour per week |   |   | Credit | Marks |
|---------------|---|---------------|------|----------------------------------|---|---|--------|-------|
|               |   |               |      | L                                | T | P |        |       |
| <b>C3</b>     | <b>C3T: Real Analysis</b>                                 | Core Course-3 |      | 5                                | 1 | 0 | 6      | 75    |
| <b>C4</b>     | <b>C 4T: Differential Equations &amp; Vector Calculus</b> | Core Course-4 |      | 5                                | 1 | 0 | 6      | 75    |
| <b>GE-2</b>   | GE-2  | GE            |      |                                  |   |   | 4/5    | 75    |
|               | GE-2  | GE            |      |                                  |   |   | 2/1    |       |
| <b>AECC-2</b> | Environmental Studies                                     | AECC          |      |                                  |   |   | 4      | 100   |
|               |   |               |      | <b>Total Credits = 22</b>        |   |   |        |       |

**L=Lecture, T=Tutorial, P=Practical**

**AECC- Ability Enhancement Compulsory Course:** Environmental Studies.

### Interdisciplinary/Generic Elective (GE) from other Department

[Four papers are to be taken and each paper will be of 6 credits]:

Papers are to be taken from any of the following discipline:

**Physics/Chemistry/Computer Sc/Statistics /Geology/Electronics/Economics  
/Physiology /Bio-technology**

**Semester-II**  
**Core Course**

**Core -3**

**CC-3: Real Analysis**

**Credits 06**

**C3T : Real Analysis**

**Real Analysis**

**Unit 1**

Review of algebraic and order properties of  $\mathbb{R}$ ,  $\varepsilon$ -neighborhood of a point in  $\mathbb{R}$ . Idea of countable sets, uncountable sets and uncountability of  $\mathbb{R}$ . Bounded above sets, bounded below sets, bounded sets, unbounded sets. Suprema and infima. Completeness property of  $\mathbb{R}$  and its equivalent properties. The Archimedean property, density of rational (and Irrational) numbers in  $\mathbb{R}$ , intervals. Limit points of a set, isolated points, open set, closed set, derived set, illustrations of Bolzano-Weierstrass theorem for sets, compact sets in  $\mathbb{R}$ , Heine-Borel Theorem.

**Unit 2**

Sequences, bounded sequence, convergent sequence, limit of a sequence,  $\liminf$ ,  $\limsup$ . Limit theorems. Monotone sequences, monotone convergence theorem. Subsequences, divergence criteria. Monotone subsequence theorem (statement only), Bolzano Weierstrass theorem for sequences. Cauchy sequence, Cauchy's convergence criterion.

**Unit 3**

Infinite series, convergence and divergence of infinite series, Cauchy criterion, tests for convergence: comparison test, limit comparison test, ratio test, Cauchy's nth root test, integral test. Alternating series, Leibniz test. Absolute and conditional convergence.

**Unit 4**

Graphical Demonstration (Teaching aid)

1. Plotting of recursive sequences.
2. Study the convergence of sequences through plotting.
3. Verify Bolzano-Weierstrass theorem through plotting of sequences and hence identify convergent subsequences from the plot.
4. Study the convergence/divergence of infinite series by plotting their sequences of partial sum.
5. Cauchy's root test by plotting nth roots.
6. Ratio test by plotting the ratio of nth and (n+1)th term.

## Reference Books

- R.G. Bartle and D. R. Sherbert, Introduction to Real Analysis, 3rd Ed., John Wiley and Sons (Asia) Pvt. Ltd., Singapore, 2002.
- Gerald G. Bilodeau , Paul R. Thie, G.E. Keough, An Introduction to Analysis, 2nd Ed., Jones& Bartlett, 2010.
- Brian S. Thomson, Andrew. M. Bruckner and Judith B. Bruckner, Elementary Real Analysis, Prentice Hall, 2001.
- S.K. Berberian, a First Course in Real Analysis, Springer Verlag, New York, 1994.
- T. Apostol, Mathematical Analysis, Narosa Publishing House
- Courant and John, Introduction to Calculus and Analysis, Vol I, Springer
- W. Rudin, Principles of Mathematical Analysis, Tata McGraw-Hill
- Terence Tao, Analysis I, Hindustan Book Agency, 2006.
- S. Goldberg, Calculus and mathematical analysis.

## Core -4

**CC-4: Differential Equations & Vector Calculus**

**Credits 06**

**C4T: Differential Equations & Vector Calculus**

## Differential Equations & Vector Calculus

6 Credits

### Unit 1

Lipschitz condition and Picard's Theorem (Statement only). General solution of homogeneous equation of second order, principle of super position for homogeneous equation, Wronskian: its properties and applications, Linear homogeneous and non-homogeneous equations of higher order with constant coefficients, Euler's equation, method of undetermined coefficients, method of variation of parameters.

### Unit 2

Systems of linear differential equations, types of linear systems, differential operators, an operator method for linear systems with constant coefficients,

Basic Theory of linear systems in normal form, homogeneous linear systems with constant coefficients: Two Equations in two unknown functions.

### Unit 3

Equilibrium points, Interpretation of the phase plane

Power series solution of a differential equation about an ordinary point, solution about a regular singular point.

#### **Unit 4**

Triple product, introduction to vector functions, operations with vector-valued functions, limits and continuity of vector functions, differentiation and integration of vector functions.

#### **Unit 5**

Graphical demonstration (Teaching aid)

1. Plotting of family of curves which are solutions of second order differential equation.
2. Plotting of family of curves which are solutions of third order differential equation.

#### **Reference Books**

- Belinda Barnes and Glenn R. Fulford, Mathematical Modeling with Case Studies, A Differential Equation Approach using Maple and Matlab, 2nd Ed., Taylor and Francis group, London and New York, 2009.
- C.H. Edwards and D.E. Penny, Differential Equations and Boundary Value problems Computing and Modeling, Pearson Education India, 2005.
- S.L. Ross, Differential Equations, 3rd Ed., John Wiley and Sons, India, 2004.
- Martha L Abell, James P Braselton, Differential Equations with MATHEMATICA, 3rd Ed., Elsevier Academic Press, 2004.
- Murray, D., Introductory Course in Differential Equations, Longmans Green and Co.
- Boyce and Diprima, Elementary Differential Equations and Boundary Value Problems, Wiley.
- G.F. Simmons, Differential Equations, Tata Mc Graw Hill
- Marsden, J., and Tromba, Vector Calculus, McGraw Hill.
- Maity, K.C. and Ghosh, R.K. Vector Analysis, New Central Book Agency (P) Ltd. Kolkata (India).
- M.R. Spiegel, Schaum's outline of Vector Analysis.

## Generic Elective Syllabus

### GE-2 [Interdisciplinary for other department]

**GE-2 : Algebra**

**Credits 06**

**GE2T : Algebra**

**Algebra**

6 Credits

#### **Unit 1**

Polar representation of complex numbers,  $n$ th roots of unity, De Moivre's theorem for rational indices and its applications.

Theory of equations: Relation between roots and coefficients, transformation of equation, Descartes rule of signs, cubic and biquadratic equation.

Inequality: The inequality involving  $AM \geq GM \geq HM$ , Cauchy-Schwartz inequality.

#### **Unit 2**

Equivalence relations. Functions, composition of functions, Invertible functions, one to one correspondence and cardinality of a set. Well-ordering property of positive integers, division algorithm, divisibility and Euclidean algorithm. Congruence relation between integers. Principles of Mathematical induction, statement of Fundamental Theorem of Arithmetic.

#### **Unit 3**

Systems of linear equations, row reduction and echelon forms, vector equations, the matrix equation  $Ax=b$ , solution sets of linear systems, applications of linear systems, linear independence.

#### **Unit 4**

Introduction to linear transformations, matrix of a linear transformation, inverse of a matrix, characterizations of invertible matrices. Subspaces of  $\mathbb{R}^n$ , dimension of subspaces of  $\mathbb{R}^n$ , rank of a matrix, Eigen values, eigen vectors and characteristic equation of a matrix. Cayley-Hamilton theorem and its use in finding the inverse of a matrix.

#### **Reference Books**

- Titu Andreescu and Dorin Andrica, Complex Numbers from A to Z, Birkhauser, 2006.
- Edgar G. Goodaire and Michael M. Parmenter, Discrete Mathematics with Graph

Theory, 3rd Ed., Pearson Education (Singapore) P. Ltd., Indian Reprint, 2005.

- David C. Lay, Linear Algebra and its Applications, 3rd Ed., Pearson Education Asia, Indian Reprint, 2007.
- K.B. Dutta, Matrix and linear algebra.
- K. Hoffman, R. Kunze, Linear algebra.
- W.S. Burnstine and A.W. Panton, Theory of equations.

# Vidyasagar University

## Curriculum for B.Sc (Honours) in Mathematics [Choice Based Credit System]

### Semester-III

| Course                | Course Code | Name of the Subjects  | Course Type/<br>Nature     | Teaching Scheme in hour per week |   |   | Credit    | Marks      |
|-----------------------|-------------|---|----------------------------|----------------------------------|---|---|-----------|------------|
|                       |             |   |                            | L                                | T | P |           |            |
| CC-5                  |             | <b>C5T:</b> Theory of Real Functions & Introduction to Metric Space                           | Core Course - 5            | 5                                | 1 | 0 | 6         | 75         |
| CC-6                  |             | <b>C6T:</b> Group Theory 1  | Core Course - 6            | 5                                | 1 | 0 | 6         | 75         |
| CC-7                  |             | <b>C7T:</b> Numerical Methods   | Core Course - 7            | 4                                | 0 | 0 | 6         | 75         |
|                       |             | <b>C7P:</b> Numerical Methods Lab   |                            | 0                                | 0 | 4 |           |            |
| GE-3                  | TBD         |   | Generic Elective -3        |                                  |   |   | 4/5       | 75         |
|                       |             |   |                            |                                  |   |   | 2/1       |            |
| SEC-1                 |             | <b>SEC1T:</b> Logic and Sets<br><b>Or</b><br><b>SEC1T:</b> Object Oriented Programming in C++ | Skill Enhancement Course-1 | 1                                | 1 | 0 | 2         | 50         |
| <b>Semester Total</b> |             |   |                            |                                  |   |   | <b>26</b> | <b>350</b> |

**L**=Lecture, **T**= Tutorial, **P**=Practical, **CC** = Core Course, **GE**= Generic Elective, **SEC** = Skill Enhancement Course, **TBD** = to be decided

**Generic Elective (GE)( Interdisciplinary)** from other Department [**Four papers are to be taken and each paper will be of 6 credits**]:

Papers are to be taken from any of the following discipline: **Physics/Chemistry/Computer Sc/Statistics /Geology/Electronics/Economics /Physiology /Bio-technology**

**Modalities of selection of Generic Electives (GE):** A student shall have to choose **04** Generic Elective (GE1 to GE4) strictly from **02** subjects / disciplines of choice taking exactly **02** courses from each subjects of disciplines. Such a student shall have to study the curriculum of Generic Elective (GE) of a subject or discipline specified for the relevant semester.

**Semester-III**  
**Core Courses (CC)**

**CC-5: Theory of Real Functions& Introduction to Metric Space**

**Credits 06**

**C5T: Theory of Real Functions& Introduction to Metric Space**

**Theory of Real Functions & Introduction to Metric Space**

**Unit 1**

Limits of functions ( $\epsilon - \delta$  approach), sequential criterion for limits, divergence criteria. Limit theorems, one sided limits. Infinite limits and limits at infinity. Continuous functions, sequential criterion for continuity and discontinuity. Algebra of continuous functions. Continuous functions on an interval, intermediate value theorem, location of roots theorem, preservation of intervals theorem. Uniform continuity, non-uniform continuity criteria, uniform continuity theorem.

**Unit 2**

Differentiability of a function at a point and in an interval, Caratheodory's theorem, algebra of differentiable functions. Relative extrema, interior extremum theorem. Rolle's theorem. Mean value theorem, intermediate value property of derivatives, Darboux's theorem. Applications of mean value theorem to inequalities and approximation of polynomials.

**Unit 3**

Cauchy's mean value theorem. Taylor's theorem with Lagrange's form of remainder, Taylor's theorem with Cauchy's form of remainder, application of Taylor's theorem to convex functions, relative extrema. Taylor's series and Maclaurin's series expansions of exponential and trigonometric functions,  $\ln(1+x)$ ,  $1/(ax+b)$  and  $(x+1)^n$ . Application of Taylor's theorem to inequalities.

**Unit 4**

Metric spaces: Definition and examples. open and closed balls, neighbourhood, open set, interior of a set. Limit point of a set, closed set, diameter of a set, subspaces, dense sets, separable spaces.

**Reference Books**

- R. Bartle and D.R. Sherbert, Introduction to Real Analysis, John Wiley and Sons, 2003.
- K.A. Ross, Elementary Analysis: The Theory of Calculus, Springer, 2004.
- A. Mattuck, Introduction to Analysis, Prentice Hall, 1999.
- S.R. Ghorpade and B.V. Limaye, a Course in Calculus and Real Analysis, Springer, 2006.
- T. Apostol, Mathematical Analysis, Narosa Publishing House
- Courant and John, Introduction to Calculus and Analysis, Vol II, Springer
- W. Rudin, Principles of Mathematical Analysis, Tata McGraw-Hill
- Terence Tao, Analysis II, Hindustan Book Agency, 2006
- SatishShirali and Harikishan L. Vasudeva, Metric Spaces, Springer Verlag, London, 2006
- S. Kumaresan, Topology of Metric Spaces, 2nd Ed., Narosa Publishing House, 2011.

- G.F. Simmons, Introduction to Topology and Modern Analysis, McGraw-Hill, 2004.

**CC-6: Group Theory 1**  
**C6T: Group Theory 1**

**Credits 06**

**Group Theory 1**

**Unit 1**

Symmetries of a square, dihedral groups, definition and examples of groups including permutation groups and quaternion groups (through matrices), elementary properties of groups.

**Unit 2**

Subgroups and examples of subgroups, centralizer, normalizer, center of a group, product of two subgroups.

**Unit 3**

Properties of cyclic groups, classification of subgroups of cyclic groups. Cycle notation for permutations, properties of permutations, even and odd permutations, alternating group, properties of cosets, Lagrange's theorem and consequences including Fermat's Little theorem.

**Unit 4**

External direct product of a finite number of groups, normal subgroups, factor groups, Cauchy's theorem for finite abelian groups.

**Unit 5**

Group homomorphisms, properties of homomorphisms, Cayley's theorem, properties of isomorphisms. First, Second and Third isomorphism theorems.

**Reference Books**

- John B. Fraleigh, A First Course in Abstract Algebra, 7th Ed., Pearson, 2002.
- M. Artin, Abstract Algebra, 2nd Ed., Pearson, 2011.
- Joseph A. Gallian, Contemporary Abstract Algebra, 4th Ed., Narosa Publishing House, New Delhi, 1999.
- Joseph J. Rotman, An Introduction to the Theory of Groups, 4th Ed., Springer Verlag, 1995.
- I.N. Herstein, Topics in Algebra, Wiley Eastern Limited, India, 1975.
- D.S. Malik, John M. Mordeson and M.K. Sen, Fundamentals of abstract algebra.

**CC-7: Numerical Methods**

**Credits 06**

**C7T: Numerical Methods**

**Credits 04**

## **Numerical Methods**

### **Unit 1**

Algorithms. Convergence. Errors: relative, absolute. Round off. Truncation.

### **Unit 2**

Transcendental and polynomial equations: Bisection method, Newton's method, secant method, Regula-falsi method, fixed point iteration, Newton-Raphson method. Rate of convergence of these methods.

### **Unit 3**

System of linear algebraic equations: Gaussian elimination and Gauss Jordan methods. Gauss Jacobi method, Gauss Seidel method and their convergence analysis. LU decomposition

### **Unit 4**

Interpolation: Lagrange and Newton's methods. Error bounds. Finite difference operators. Gregory forward and backward difference interpolation.

Numerical differentiation: Methods based on interpolations, methods based on finite differences.

### **Unit 5**

Numerical Integration: Newton Cotes formula, Trapezoidal rule, Simpson's 1/3<sup>rd</sup> rule, Simpsons 3/8th rule, Weddle's rule, Boole's Rule. midpoint rule, Composite trapezoidal rule, composite Simpson's 1/3<sup>rd</sup> rule, Gauss quadrature formula.

The algebraic eigen value problem: Power method.

Approximation: Least square polynomial approximation.

### **Unit 6**

Ordinary differential equations: The method of successive approximations, Euler's method, the modified Euler method, Runge-Kutta methods of orders two and four.

## **Reference Books**

- Brian Bradie, A Friendly Introduction to Numerical Analysis, Pearson Education, India, 2007.
- M.K. Jain, S.R.K. Iyengar and R.K. Jain, Numerical Methods for Scientific and Engineering Computation, 6th Ed., New age International Publisher, India, 2007.
- C.F. Gerald and P.O. Wheatley, Applied Numerical Analysis, Pearson Education, India, 2008.
- Uri M. Ascher and Chen Greif, A First Course in Numerical Methods, 7th Ed., PHI Learning Private Limited, 2013.
- John H. Mathews and Kurtis D. Fink, Numerical Methods using Matlab, 4th Ed., PHI Learning Private Limited, 2012.
- Scarborough, James B., Numerical Mathematical Analysis, Oxford and IBH publishing co.

- Atkinson, K. E., An Introduction to Numerical Analysis, John Wiley and Sons, 1978.
- Yashavant Kanetkar, Let Us C , BPB Publications.

**C7P: Numerical Methods Lab**  
**Numerical Methods Lab**

**Credits 02**

**List of practical (using any software)**

1. Calculate the sum  $1/1 + 1/2 + 1/3 + 1/4 + \dots + 1/N$ .
2. Enter 100 integers into an array and sort them in an ascending order.
3. Solution of transcendental and algebraic equations by
  - i) Bisection method
  - ii) Newton Raphson method.
  - iii) Secant method.
  - iv) Regula Falsi method.
4. Solution of system of linear equations
  - i) LU decomposition method
  - ii) Gaussian elimination method
  - iii) Gauss-Jacobi method
  - iv) Gauss-Seidel method
5. Interpolation
  - i) Lagrange Interpolation
  - ii) Newton Interpolation
6. Numerical Integration
  - i) Trapezoidal Rule
  - ii) Simpson's one third rule
  - iii) Weddle's Rule
  - iv) Gauss Quadrature
7. Method of finding Eigenvalue by Power method
8. Fitting a Polynomial Function
9. Solution of ordinary differential equations
  - i) Euler method
  - ii) Modified Euler method
  - iii) Runge Kutta method

Note: For any of the CAS (Computer aided software) Data types-simple data types, floating data types, character data types, arithmetic operators and operator precedence, variables and constant declarations, expressions, input/output, relational operators, logical operators and logical expressions, control statements and loop statements, Arrays should be introduced to the students.

## Skill Enhancement Course (SEC)

### SEC-1: Logic and Sets

Credits 02

#### SEC1T: Logic and Sets

#### Logic and Sets

##### Unit 1

Introduction, propositions, truth table, negation, conjunction and disjunction. Implications, biconditional propositions, converse, contra positive and inverse propositions and precedence of logical operators. Propositional equivalence: Logical equivalences. Predicates and quantifiers: Introduction, quantifiers, binding variables and negations.

##### Unit 2

Sets, subsets, set operations and the laws of set theory and Venn diagrams. Examples of finite and infinite sets. Finite sets and counting principle. Empty set, properties of empty set. Standard set operations. classes of sets. Power set of a set.

##### Unit 3

Difference and Symmetric difference of two sets. Set identities, generalized union and intersections. Relation: Product set. Composition of relations, types of relations, partitions, equivalence Relations with example of congruence modulo relation. Partial ordering relations, n- ary relations.

#### Reference Books

- R.P. Grimaldi, Discrete Mathematics and Combinatorial Mathematics, Pearson Education, 1998.
- P.R. Halmos, Naive Set Theory, Springer, 1974.
- E. Kamke, Theory of Sets, Dover Publishers, 1950.

Or

### SEC-1: Object Oriented Programming in C++

Credits 02

#### SEC1T: Object Oriented Programming in C++

#### Object Oriented Programming in C++

##### Unit 1

Programming paradigms, characteristics of object oriented programming languages, brief history of C++, structure of C++ program, differences between C and C++, basic C++ operators, Comments, working with variables, enumeration, arrays and pointer.

##### Unit 2

Objects, classes, constructor and destructors, friend function, inline function, encapsulation, data abstraction, inheritance, polymorphism, dynamic binding, operator overloading, method overloading, overloading arithmetic operator and comparison operators.

### Unit 3

Template class in C++, copy constructor, subscript and function call operator, concept of namespace and exception handling.

#### Reference Books

- A. R. Venugopal, Rajkumar, and T. Ravishanker, Mastering C++, TMH, 1997.
- S. B. Lippman and J. Lajoie, C++ Primer, 3rd Ed., Addison Wesley, 2000.
- Bruce Eckel, Thinking in C++, 2nd Ed., President, Mindview Inc., Prentice Hall.
- D. Parsons, Object Oriented Programming with C++, BPB Publication.
- Bjarne Stroustrup, The C++ Programming Language, 3rd Ed., Addison Welsley.
- E. Balaguruswami, Object Oriented Programming In C++, Tata McGrawHill
- Herbert Schildt, C++, The Complete Reference, Tata McGrawHill.

## Generic Elective Syllabus GE-3 [Interdisciplinary for other department]

**GE-3: Differential Equations & Vector Calculus**

**Credits 06**

**GE3T: Differential Equations & Vector Calculus**

### Differential Equations

#### Unit 1

Lipschitz condition and Picard's Theorem (Statement only). General solution of homogeneous equation of second order, principle of super position for homogeneous equation, Wronskian: its properties and applications, Linear homogeneous and non-homogeneous equations of higher order with constant coefficients, Euler's equation, method of undetermined coefficients, method of variation of parameters.

#### Unit 2

Systems of linear differential equations, types of linear systems, differential operators, an operator method for linear systems with constant coefficients, Basic Theory of linear systems in normal form, homogeneous linear systems with constant coefficients: Two Equations in two unknown functions.

#### Unit 3

Equilibrium points, Interpretation of the phase plane  
Power series solution of a differential equation about an ordinary point, solution about a regular singular point.

#### Unit 4

Triple product, introduction to vector functions, operations with vector-valued functions, limits and continuity of vector functions, differentiation and integration of vector functions.

#### Unit 5

Graphical demonstration (Teaching aid)

1. Plotting of family of curves which are solutions of second order differential equation.

2. Plotting of family of curves which are solutions of third order differential equation.

### Reference Books

- Belinda Barnes and Glenn R. Fulford, Mathematical Modeling with Case Studies, A Differential Equation Approach using Maple and Matlab, 2nd Ed., Taylor and Francis group, London and New York, 2009.
- C.H. Edwards and D.E. Penny, Differential Equations and Boundary Value problems Computing and Modeling, Pearson Education India, 2005.
- S.L. Ross, Differential Equations, 3rd Ed., John Wiley and Sons, India, 2004.
- Martha L Abell, James P Braselton, Differential Equations with MATHEMATICA, 3rd Ed., Elsevier Academic Press, 2004.
- Murray, D., Introductory Course in Differential Equations, Longmans Green and Co.
- Boyce and Diprima, Elementary Differential Equations and Boundary Value Problems, Wiley.
- G.F.Simmons, Differential Equations, Tata Mc Graw Hill
- Marsden, J., and Tromba, Vector Calculus, McGraw Hill.
- Maity, K.C. and Ghosh, R.K. Vector Analysis, New Central Book Agency (P) Ltd. Kolkata (India).
- M.R. Spiegel, Schaum's outline of Vector Analysis.